

3-9-1 Inequalities

Sometimes its hard to remember which way the symbols $<$ and $>$ go. Think "the alligator eats the larger number." This is a little childish, but you won't forget again.

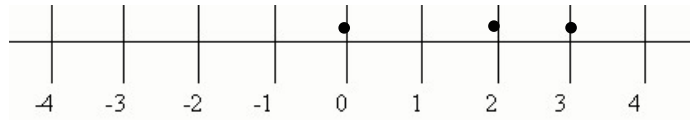


8 $<$ 13 8 $<$ 13 Eight is less than 13.

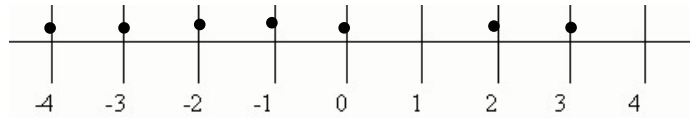


Negative five is greater than negative twenty-three. -5 $>$ -23 -5 $>$ -23

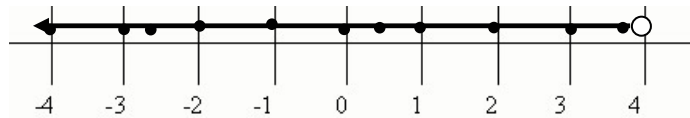
Some numbers that fit for the inequality $x < 4$ are 3, 2, and 0. These are plotted below.



All the negative numbers also satisfy the inequality.

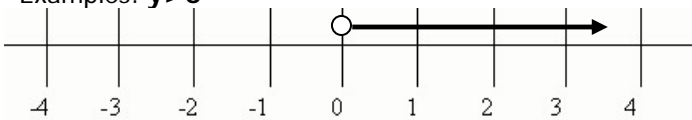


$\frac{1}{2}$, $3\frac{3}{4}$, $-\frac{2}{3}$, 3.9, 3.99, and 3.999 also work. 4 is not less than 4 so 4 is not part of the solution. An open circle illustrates getting close but not including the number the circle is on.

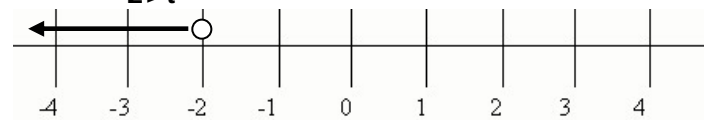


When \leq and \geq are involved, use a closed circle to indicate the "or equal to" part of the symbol.

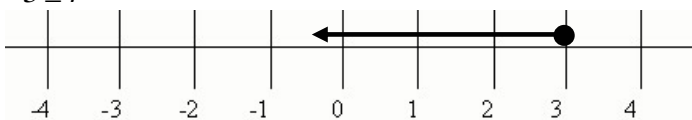
Examples: $y > 0$



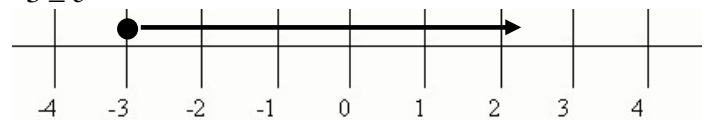
$-2 > t$



$3 \geq r$

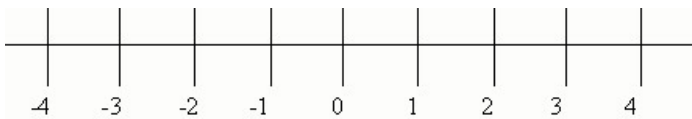


$-3 \leq e$

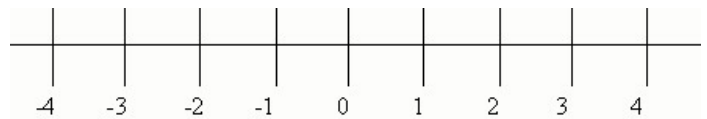


Practice: Plot the solution for each inequality.

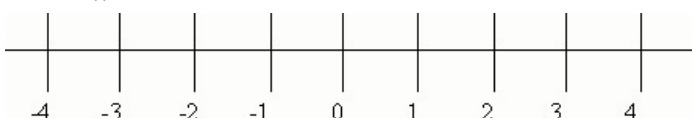
$0 \geq r$



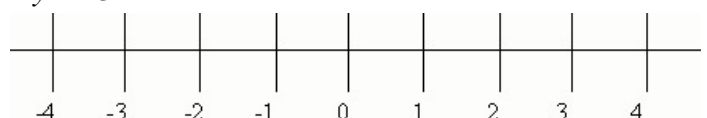
$0 < u$



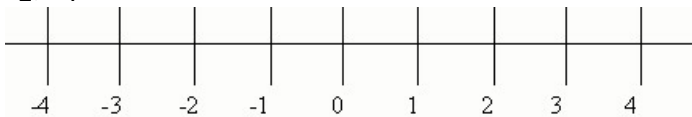
$-2 \leq x$



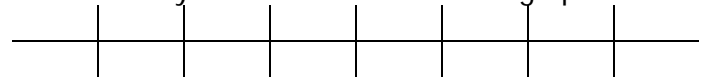
$y \leq -3$



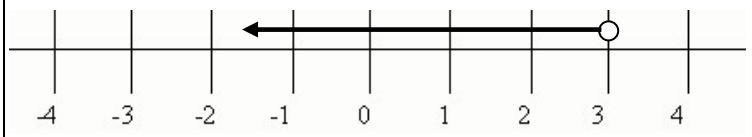
$z > -1$



$x < 30$ Fill in your own numbers on the graph below.

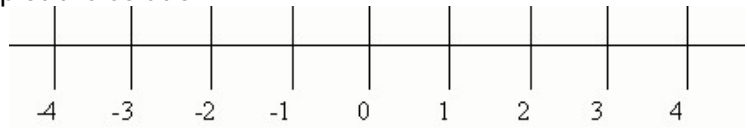


Notice the steps are the same for solving both an equation and an inequality.

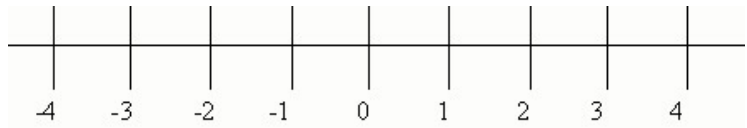
$\begin{array}{r} 3x-7=2 \\ +7 \quad +7 \\ \hline 3x=9 \\ x=3 \end{array}$	$\begin{array}{r} 3x-7 < 2 \\ +7 \quad +7 \\ \hline 3x < 9 \\ x < 3 \end{array}$	The solution is then plotted.	
--	--	-------------------------------	--

Practice: Solve the following inequalities and plot the solution.

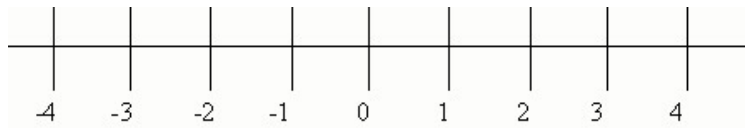
a) $6 < 2x$



b) $4 > t+6$



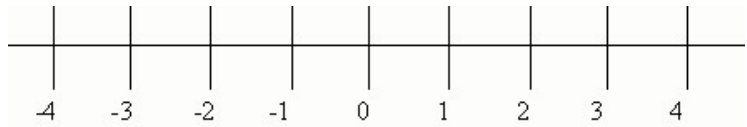
c) $7r \leq 21$



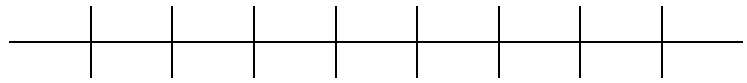
d) $s - 8 \geq -12$



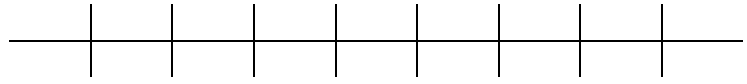
e) $2 + 3x \geq 11$



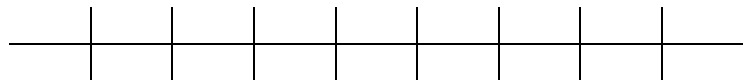
f) $44 < 2x - 90$ Label the number line.



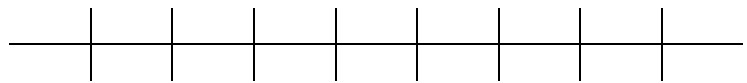
g) $10y - 30 > 15$



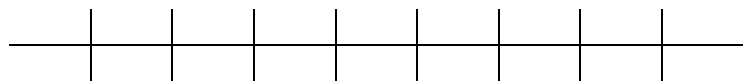
h) $3(2x - 12) < 14$



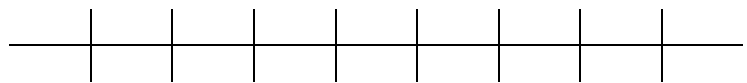
i) $-100 \leq 2(w - 7)$



j) $6x - 10 < 3x + 26$

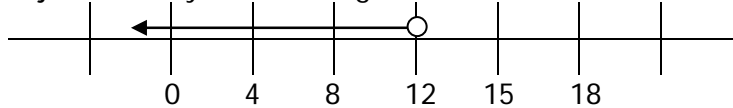


k) $2w - 16 > 5w + 12$



The last two questions, j and k, only have one right answer. Look at the solution of j.

$$\begin{array}{r}
 6x - 10 < 3x + 26 \\
 -3x \quad -3x \\
 \hline
 3x - 10 < 26 \\
 +10 \quad +10 \\
 \hline
 3x < 36 \\
 \frac{3x}{3} < \frac{36}{3} \\
 x < 12
 \end{array}$$



No matter which way the problem is done the answer must be the same.

When both sides of an inequality are divided by a negative number (or multiplied), the inequality symbol is flipped. It is changed to the other symbol.

$$\begin{array}{r}
 6x - 10 < 3x + 26 \\
 -6x \quad -6x \\
 \hline
 -10 < -3x + 26 \\
 -26 \quad -26 \\
 \hline
 -36 < -3x \\
 \frac{-36}{-3} < \frac{-3x}{-3} \\
 12 < ??? > x \\
 12 > x
 \end{array}$$

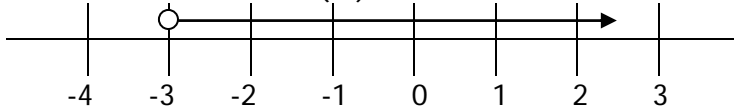
Think through the solution set in the integers for $-x < 3$.

$-(-2) < 3$ is true so -2 is in the solution. $-(-1) < 3$ is true so -1 is in the solution.

$-2, -1, 0, 1,$ and 2 are in the solution.

Is 4 in the solution? $-4 < 3$ is true so 4 is in the solution set. Try $5, 6$ and 7 .

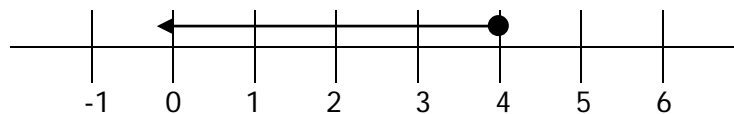
Is -4 in the solution? $-(-4) < 3$ is NOT true so -4 is not in the solution. Try $-5, -6,$ and -7 .



The solution is $x > -3$. Start with $-x < 3$. Divide both sides by -1 and flip the inequality.

Example:

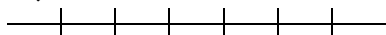
$$\begin{array}{r}
 3 - 5x \geq -17 \\
 -3 \quad -3 \\
 \hline
 -5x \geq -20 \\
 \frac{-5x}{-5} \leq \frac{-20}{-5} \\
 x \leq 4
 \end{array}$$



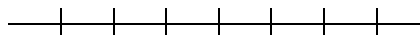
Add 3 didn't flip the sign, but divide by -5 flips the sign.

Practice: Graph the solution set of the following.

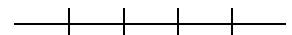
a) $-t < 8$



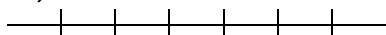
$-9 < -r$



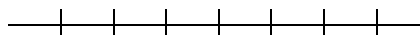
$5 < 8e - 10e$



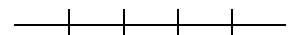
b) $4 - x \leq 12$



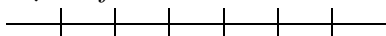
$15 \leq 7 - t$



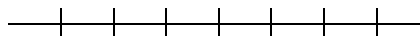
$4 - 5x \leq 54$



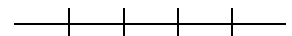
c) $-3f > 12$



$-28 \leq -7w$



$-4 \geq -12a$



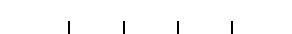
d) $-\frac{w}{5} \leq 30$



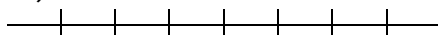
$-3\frac{2}{3} - t > 5\frac{1}{2}$



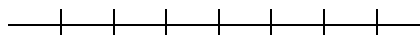
$-2\frac{3}{4} \geq -8\frac{2}{3} - \frac{3}{4}k$



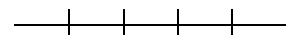
e) $7 - 2x < 15$



$-23 < 4 - 9x$



$3 \geq -12 - 5a$



f) $x - 3(2 + x) > 18$



$15 - 8(2x + 6) \leq 42$



$27 > 8x - 3(4x - 6)$

